



# PHYSICAL SCIENCES

Question Booklet Sl. No.

Name & Signature of the Invigilator **PAPER – II** OMR Answer Sheet No. :

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020527

**CODE-02** Roll No. :

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(in figures as in Hall Ticket)

Roll Number in words : .....

Time : 2 Hours]

No. of Printed Pages : 32

[Maximum Marks : 200

## Instructions for the Candidates

- Write your Roll Number in the space provided on the top of this page.
- This paper consists of **one hundred (100)** multiple choice type of questions. **All** questions are compulsory.
- At the commencement of examination, the question booklet will be given to you. In the first 5 minutes, you are requested to open the booklet and compulsorily examine it as below :
  - To have access to the Question Booklet, tear off the paper seal on the edge of this cover page. Do not accept a booklet without sticker seal and do not accept an open booklet.
  - Tally the number of pages and number of questions in the booklet with the information printed on the cover page. Faulty booklets due to pages/questions missing or duplicate or not in serial order or any other discrepancy should be got replaced immediately by a correct booklet from the invigilator within the period of 5 minutes. Afterwards, neither the Question Booklet will be replaced nor any extra time will be given.
  - After this verification is over, the Test Booklet Number should be entered on the OMR Answer Sheet and the OMR Answer Sheet Number should be entered on this Test Booklet.
- Each item has four alternative responses marked (A), (B), (C) and (D). You have to darken the oval as indicated below on the correct response against each item.
 

**Example:** (A) (B) (C) (D) where (B) is the correct response.
- Your responses to the items are to be indicated on the OMR Answer Sheet under Paper – II only. If you mark your response at any place other than in the oval in the OMR Answer Sheet, it will not be evaluated.
- Rough Work is to be done in the end of this booklet.
- If you write your Name, Roll Number, Phone Number or put any mark on any part of the OMR Answer Sheet, except for the space allotted for the relevant entries, which may disclose your identity, or use abusive language or employ any other unfair means, such as change of response by scratching or using white fluid, you will render yourself liable to disqualification.
- You have to return the original OMR Answer Sheet to the invigilator at the end of the examination compulsorily and must not carry it with you outside the Examination Hall. You are however, allowed to carry original question booklet and duplicate copy of OMR Answer Sheet on conclusion of examination.
- Use only Blue/Black Ball point pen.
- Use of any calculator or any electronic devices or log table etc., are prohibited.
- There shall be no negative marking.

## પરીક્ષાર્થીઓ માટે સૂચનાઓ

- આ પાનાની ટોચ પર દર્શાવેલી જગ્યામાં તમારો રોલ નંબર લખો.
- આ પ્રશ્નપત્રમાં બહુવૈકલ્પિક ઉત્તરો પ્રશ્નવલ્લભ સ્કે (100) પ્રશ્નો આપેલા છે. બધા જ પ્રશ્નો ફરજિયાત છે.
- પરીક્ષાની શરૂઆતમાં આપને પ્રશ્નપુસ્તિકા આપવામાં આવશે. પ્રથમ પાંચ (૫) મિનિટ દરમિયાન તમારે પ્રશ્નપુસ્તિકા ખોલી અને ફરજિયાતપણે નીચે મુજબ પરીક્ષણ કરવું :
  - પ્રશ્નપુસ્તિકાનો વપરાશ કરવા માટે આ કવર પૃષ્ઠની ધાર પર આપેલ સીલ સ્ટીકર ફાડી નાખો. કોઈપણ સંજોગોમાં સીલ સ્ટીકર વગરની કે ખુલ્લી પ્રશ્નપુસ્તિકા સ્વીકારશો નહીં.
  - કવર પૃષ્ઠ પર છપાયેલ નિર્દેશાનુસાર પ્રશ્નપુસ્તિકાના પ્રશ્નો, પૃષ્ઠો અને સંખ્યાને બરાબર ચકાસી લો. ખામીયુક્ત પ્રશ્નપુસ્તિકા કે જેમાં પ્રશ્નો/ પૃષ્ઠો ઓછાં હોય, બે વાર છપાયા હોય, અનુક્રમમાં અથવા અન્ય કોઈ ફરક હોય અર્થાત કોઈપણ સંજોગોમાં ખામીયુક્ત પ્રશ્નપુસ્તિકા સ્વીકારશો નહીં. અને જો ખામીયુક્ત પ્રશ્નપુસ્તિકા મળી હોય તો નિરીક્ષક પાસેથી તુરંત જ બીજી સારી પ્રશ્નપુસ્તિકા મેળવી લેવી. આ માટે ઉમેદવારને પાંચ (૫) મિનિટનો સમયગાળો આપવામાં આવશે. પછીથી, પ્રશ્નપુસ્તિકા બદલવામાં આવશે નહીં કે કોઈ વધારાનો સમયગાળો આપવામાં આવશે નહીં.
  - આ ચકાસણી સમાપ્ત થાય પછી, પ્રશ્નપુસ્તિકાનો નંબર OMR જવાબ પત્રક પર લખવો અને OMR જવાબ પત્રકનો નંબર પ્રશ્નપુસ્તિકા પર લખવો.
- પ્રત્યેક પ્રશ્ન માટે ચાર જવાબ વિકલ્પ (A), (B), (C) અને (D) આપવામાં આવેલ છે. તમારે સાચા જવાબના ઓવલ (oval)ને નીચે આપેલ ઉદાહરણ મુજબ પેનથી ભરીને સંપૂર્ણ કાળું કરવાનું રહેશે.
 

ઉદાહરણ : (A) (B) (C) (D) કે જ્યાં (B) સાચો જવાબ છે.
- આ પ્રશ્નપુસ્તિકાના પ્રશ્નોના જવાબ અલગથી આપવામાં આવેલ OMR જવાબ પત્રકમાં પેપર-IIલખેલ વિભાગમાં જ અંકિત કરવા. જો આપ OMR જવાબ પત્રકમાં આપેલ ઓવલ (oval)સિવાય અન્ય સ્થાને જવાબ અંકિત કરશો તો તે જવાબનું મૂલ્યાંકન કરવામાં આવશે નહીં.
- કાચું કામ (Rough work) પ્રશ્નપુસ્તિકાના અંતિમ પૃષ્ઠ પર કરવું.
- જો આપ OMR જવાબ પત્રક નિયત જગ્યા સિવાય અન્ય કોઈપણ સ્થાને, આપનું નામ, રોલ નંબર, ફોન નંબર અથવા એવું કોઈ ચિહ્ન જેનાથી તમારી ઓળખ થઈ શકે, અંકિત કરશો અથવા અલગ ભાષાનો પ્રયોગ કરો, અથવા અન્ય કોઈ અનુચિત સાધનોનો ઉપયોગ કરો, જેમકે અંકિત કરી દીધેલ જવાબ બૂંસી નાખવો કે સફેદ શાહીનો ઉપયોગ કરી બદલશો તો આપને પરીક્ષા માટે અયોગ્ય જાહેર કરવામાં આવશે.
- પરીક્ષા સમય પૂરો થઈ ગયા બાદ ઓરીજીનલ OMR જવાબ પત્રક જે તે નિરીક્ષકને ફરજિયાત સોંપી દેવું અને કોઈ પણ સંજોગોમાં તે પરીક્ષા ખંડની બહાર લઈ જવું નહીં. પરીક્ષા પૂર્ણ થયા બાદ ઉમેદવાર ઓરીજીનલ પ્રશ્નપુસ્તિકા અને OMR જવાબ પત્રકની ડુપ્લિકેટ કોપી પોતાની સાથે લઈ જઈ શકે છે.
- માત્ર કાળી / ભૂરી બોલ પોઈન્ટ પેન વાપરવી.
- કેલ્ક્યુલેટર, લોગ ટેબલ અને અન્ય ઇલેક્ટ્રોનિક યંત્રોનો ઉપયોગ કરવાની મનાઈ છે.
- ખોટા જવાબ માટે નકારાત્મક ગુણાંકન પ્રથા નથી.

SEAL



DO NOT WRITE HERE



# LOGARITHMS

	0	1	2	3	4	5	6	7	8	9	Mean Differences								
											1	2	3	4	5	6	7	8	9
10	0000	0043	0086	0128	0170	0212	0253	0294	0334	0374	4	8	12	17	21	25	29	33	37
11	0414	0453	0492	0531	0569	0607	0645	0682	0719	0755	4	8	11	15	19	23	26	30	34
12	0792	0828	0864	0899	0934	0969	1004	1038	1072	1106	3	7	10	14	17	21	24	28	31
13	1139	1173	1206	1239	1271	1303	1335	1367	1399	1430	3	6	10	13	16	19	23	26	29
14	1481	1492	1523	1553	1584	1614	1644	1673	1703	1732	3	6	9	12	15	18	21	24	27
15	1761	1790	1818	1847	1875	1903	1931	1959	1987	2014	3	6	8	11	14	17	20	22	25
16	2041	2068	2095	2122	2148	2175	2201	2227	2253	2279	3	5	8	11	13	16	18	21	24
17	2304	2330	2355	2380	2405	2430	2455	2480	2504	2529	2	5	7	10	12	15	17	20	22
18	2553	2577	2601	2625	2648	2672	2695	2718	2742	2765	2	5	7	9	12	14	16	19	21
19	2786	2810	2833	2856	2878	2900	2923	2945	2967	2989	2	4	7	9	11	13	16	18	20
20	3010	3032	3054	3075	3096	3118	3139	3160	3181	3201	2	4	6	8	11	13	15	17	19
21	3222	3243	3263	3284	3304	3324	3345	3365	3385	3404	2	4	6	8	10	12	14	16	18
22	3424	3444	3464	3483	3502	3522	3541	3560	3579	3598	2	4	6	8	10	12	14	15	17
23	3617	3636	3655	3674	3692	3711	3729	3747	3765	3784	2	4	6	7	9	11	13	15	17
24	3802	3820	3838	3856	3874	3892	3909	3927	3945	3962	2	4	5	7	9	11	12	14	16
25	3979	3997	4014	4031	4048	4065	4082	4099	4116	4133	2	3	5	7	9	10	12	14	15
26	4150	4166	4183	4200	4216	4232	4249	4265	4281	4298	2	3	5	7	8	10	11	13	15
27	4314	4330	4346	4362	4378	4393	4409	4425	4440	4456	2	3	5	6	8	9	11	13	14
28	4472	4487	4502	4518	4533	4548	4564	4579	4594	4609	2	3	5	6	8	9	11	12	14
29	4624	4639	4654	4669	4683	4698	4713	4728	4742	4757	1	3	4	6	7	9	10	12	13
30	4771	4786	4800	4814	4829	4843	4857	4871	4886	4900	1	3	4	6	7	9	10	11	13
31	4914	4928	4942	4955	4969	4983	4997	5011	5024	5038	1	3	4	6	7	8	10	11	12
32	5051	5065	5079	5092	5105	5119	5132	5145	5159	5172	1	3	4	5	7	8	9	11	12
33	5185	5198	5211	5224	5237	5250	5263	5276	5289	5302	1	3	4	5	6	8	9	10	12
34	5315	5328	5340	5353	5366	5378	5391	5403	5416	5428	1	3	4	5	6	8	9	10	11
35	5441	5453	5465	5478	5490	5502	5514	5527	5539	5551	1	2	4	5	6	7	9	10	11
36	5563	5575	5587	5599	5611	5623	5635	5647	5658	5670	1	2	4	5	6	7	8	10	11
37	5682	5694	5705	5717	5729	5740	5752	5763	5775	5786	1	2	3	5	6	7	8	9	10
38	5798	5809	5821	5832	5843	5855	5866	5877	5888	5899	1	2	3	5	6	7	8	9	10
39	5911	5922	5933	5944	5955	5966	5977	5988	5999	6010	1	2	3	4	5	7	8	9	10
40	6021	6031	6042	6053	6064	6075	6085	6096	6107	6117	1	2	3	4	5	6	8	9	10
41	6128	6138	6149	6160	6170	6180	6191	6201	6212	6222	1	2	3	4	5	6	7	8	9
42	6232	6243	6253	6263	6274	6284	6294	6304	6314	6325	1	2	3	4	5	6	7	8	9
43	6335	6345	6355	6365	6375	6385	6395	6405	6415	6425	1	2	3	4	5	6	7	8	9
44	6435	6444	6454	6464	6474	6484	6493	6503	6513	6522	1	2	3	4	5	6	7	8	9
45	6532	6542	6551	6561	6571	6580	6590	6599	6609	6618	1	2	3	4	5	6	7	8	9
46	6628	6637	6646	6656	6665	6675	6684	6693	6702	6712	1	2	3	4	5	6	7	7	8
47	6721	6730	6739	6749	6758	6767	6776	6785	6794	6803	1	2	3	4	5	5	6	7	8
48	6812	6821	6830	6839	6848	6857	6866	6875	6884	6893	1	2	3	4	4	5	6	7	8
49	6902	6911	6920	6928	6937	6946	6955	6964	6972	6981	1	2	3	4	4	5	6	7	8
50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067	1	2	3	3	4	5	6	7	8
51	7076	7084	7093	7101	7110	7118	7126	7135	7143	7152	1	2	3	3	4	5	6	7	8
52	7160	7168	7177	7185	7193	7202	7210	7218	7226	7235	1	2	2	3	4	5	6	7	7
53	7243	7251	7259	7267	7275	7284	7292	7300	7308	7316	1	2	2	3	4	5	6	6	7
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396	1	2	2	3	4	5	6	6	7

No.  
x = 3.14159  
e = 2.71828

log  
0.49715  
0.43429

$\ln x = \log_e x = (1/M) \log_{10} x$   
 $\log x = \log_{10} x = M \log_e x$

No.  
(1/M) = 2.30259  
M = 0.43429

log  
0.36222  
1/0.3778



### LOGARITHMS

	0	1	2	3	4	5	6	7	8	9	Mean Differences								
											1	2	3	4	5	6	7	8	9
55	7404	7412	7419	7427	7435	7443	7451	7459	7466	7474	1	2	2	3	4	5	5	6	7
56	7482	7490	7497	7505	7513	7520	7528	7536	7543	7551	1	2	2	3	4	5	5	6	7
57	7559	7566	7574	7582	7589	7597	7604	7612	7619	7627	1	2	2	3	4	5	5	6	7
58	7634	7642	7649	7657	7664	7672	7679	7686	7694	7701	1	1	2	3	4	4	5	6	7
59	7709	7716	7723	7731	7738	7745	7752	7760	7767	7774	1	1	2	3	4	4	5	6	7
60	7782	7789	7796	7803	7810	7818	7825	7832	7839	7846	1	1	2	3	4	4	5	6	6
61	7859	7866	7868	7875	7882	7889	7896	7903	7910	7917	1	1	2	3	4	4	5	6	6
62	7924	7931	7938	7945	7952	7959	7966	7973	7980	7987	1	1	2	3	3	4	5	6	6
63	7993	8000	8007	8014	8021	8028	8035	8041	8048	8055	1	1	2	3	3	4	5	6	6
64	8062	8069	8075	8082	8089	8096	8102	8109	8116	8122	1	1	2	3	3	4	5	6	6
65	8129	8136	8142	8149	8156	8162	8169	8176	8182	8189	1	1	2	3	3	4	5	6	6
66	8195	8202	8209	8215	8222	8228	8235	8241	8248	8254	1	1	2	3	3	4	5	6	6
67	8261	8267	8274	8280	8287	8293	8299	8306	8312	8319	1	1	2	3	3	4	5	6	6
68	8325	8331	8338	8344	8351	8357	8363	8370	8376	8382	1	1	2	3	3	4	4	5	6
69	8388	8395	8401	8407	8414	8420	8426	8432	8439	8445	1	1	2	2	3	4	4	5	6
70	8451	8457	8463	8470	8476	8482	8488	8494	8500	8506	1	1	2	2	3	4	4	5	6
71	8513	8519	8525	8531	8537	8543	8549	8555	8561	8567	1	1	2	2	3	4	4	5	5
72	8573	8579	8585	8591	8597	8603	8609	8615	8621	8627	1	1	2	2	3	4	4	5	5
73	8633	8639	8645	8651	8657	8663	8669	8675	8681	8686	1	1	2	2	3	4	4	5	5
74	8692	8698	8704	8710	8716	8722	8727	8733	8739	8745	1	1	2	2	3	4	4	5	5
75	8751	8756	8762	8768	8774	8779	8785	8791	8797	8802	1	1	2	2	3	3	4	5	5
76	8808	8814	8820	8825	8831	8837	8842	8848	8854	8859	1	1	2	2	3	3	4	5	5
77	8865	8871	8876	8882	8887	8893	8899	8904	8910	8915	1	1	2	2	3	3	4	4	5
78	8921	8927	8932	8938	8943	8949	8954	8960	8965	8971	1	1	2	2	3	3	4	4	5
79	8976	8982	8987	8993	8998	9004	9009	9015	9020	9025	1	1	2	2	3	3	4	4	5
80	9031	9036	9042	9047	9053	9058	9063	9069	9074	9079	1	1	2	2	3	3	4	4	5
81	9085	9090	9096	9101	9106	9112	9117	9122	9128	9133	1	1	2	2	3	3	4	4	5
82	9138	9143	9149	9154	9159	9165	9170	9175	9180	9186	1	1	2	2	3	3	4	4	5
83	9191	9196	9201	9206	9212	9217	9222	9227	9232	9238	1	1	2	2	3	3	4	4	5
84	9243	9248	9253	9258	9263	9269	9274	9279	9284	9289	1	1	2	2	3	3	4	4	5
85	9294	9299	9304	9309	9315	9320	9325	9330	9335	9340	1	1	2	2	3	3	4	4	5
86	9345	9350	9355	9360	9365	9370	9375	9380	9385	9390	1	1	2	2	3	3	4	4	5
87	9395	9400	9405	9410	9415	9420	9425	9430	9435	9440	0	1	1	2	2	3	3	4	4
88	9445	9450	9455	9460	9465	9469	9474	9479	9484	9489	0	1	1	2	2	3	3	4	4
89	9494	9499	9504	9509	9513	9518	9523	9528	9533	9538	0	1	1	2	2	3	3	4	4
90	9542	9547	9552	9557	9562	9566	9571	9576	9581	9586	0	1	1	2	2	3	3	4	4
91	9590	9595	9600	9605	9609	9614	9619	9624	9628	9633	0	1	1	2	2	3	3	4	4
92	9638	9643	9647	9652	9657	9661	9666	9671	9675	9680	0	1	1	2	2	3	3	4	4
93	9685	9689	9694	9699	9703	9708	9713	9717	9722	9727	0	1	1	2	2	3	3	4	4
94	9731	9736	9741	9745	9750	9754	9759	9763	9768	9773	0	1	1	2	2	3	3	4	4
95	9777	9782	9786	9791	9795	9800	9805	9809	9814	9818	0	1	1	2	2	3	3	4	4
96	9823	9827	9832	9836	9841	9845	9850	9854	9859	9863	0	1	1	2	2	3	3	4	4
97	9868	9872	9877	9881	9886	9890	9894	9899	9903	9908	0	1	1	2	2	3	3	4	4
98	9912	9917	9921	9926	9930	9934	9939	9943	9948	9952	0	1	1	2	2	3	3	4	4
99	9956	9961	9965	9969	9974	9978	9983	9987	9991	9996	0	1	1	2	2	3	3	4	4

$p$	1	2	3	4	5	6	7	8	9	10
$\log e^p$	0.4343	0.8686	1.3029	1.7372	2.1715	2.6058	3.0401	3.4744	3.9087	4.3429
$\log e^{-p}$	1.5657	1.1314	2.8971	2.2628	3.8285	3.3942	4.0599	4.5256	4.0913	5.6571

ANTILOGARITHMS

	0	1	2	3	4	5	6	7	8	9
00	1000	1002	1005	1007	1009	1012	1014	1016	1019	1021
01	1023	1026	1028	1030	1033	1035	1038	1040	1042	1045
02	1047	1050	1052	1054	1057	1059	1062	1064	1067	1069
03	1072	1074	1076	1079	1081	1084	1086	1089	1091	1094
04	1096	1099	1102	1104	1107	1109	1112	1114	1117	1119
05	1122	1125	1127	1130	1132	1135	1138	1140	1143	1146
06	1148	1151	1153	1156	1158	1161	1164	1167	1169	1172
07	1175	1178	1180	1183	1185	1188	1191	1194	1197	1199
08	1202	1205	1208	1211	1213	1216	1219	1222	1225	1227
09	1230	1233	1236	1239	1242	1245	1247	1250	1253	1256
10	1259	1262	1265	1268	1271	1274	1277	1279	1282	1285
11	1288	1291	1294	1297	1300	1303	1306	1309	1312	1315
12	1318	1321	1324	1327	1330	1334	1337	1340	1343	1346
13	1349	1352	1355	1358	1361	1365	1368	1371	1374	1377
14	1380	1384	1387	1390	1393	1396	1400	1403	1406	1409
15	1413	1416	1419	1422	1425	1429	1432	1435	1439	1442
16	1445	1449	1452	1455	1459	1462	1466	1469	1472	1476
17	1479	1483	1487	1490	1493	1496	1500	1503	1507	1510
18	1514	1518	1521	1524	1528	1531	1535	1538	1542	1545
19	1549	1552	1556	1560	1563	1567	1570	1574	1578	1581
20	1585	1588	1592	1596	1600	1603	1607	1611	1614	1618
21	1622	1626	1629	1633	1637	1641	1644	1648	1652	1656
22	1660	1664	1667	1671	1675	1679	1683	1687	1690	1694
23	1698	1702	1706	1710	1714	1718	1722	1726	1730	1734
24	1738	1742	1746	1750	1754	1758	1762	1766	1770	1774
25	1778	1782	1786	1790	1794	1798	1802	1807	1811	1816
26	1820	1824	1828	1833	1837	1841	1845	1849	1854	1858
27	1862	1866	1871	1875	1879	1884	1888	1892	1897	1901
28	1905	1910	1914	1919	1923	1928	1932	1936	1941	1945
29	1950	1954	1959	1963	1968	1972	1977	1982	1986	1991
30	1995	2000	2004	2009	2014	2018	2023	2028	2032	2037
31	2042	2046	2051	2056	2061	2066	2070	2075	2080	2084
32	2089	2094	2099	2104	2109	2113	2118	2123	2128	2133
33	2138	2143	2148	2153	2158	2163	2168	2173	2178	2183
34	2188	2193	2198	2203	2208	2213	2218	2223	2228	2234
35	2239	2244	2249	2254	2259	2264	2270	2275	2280	2286
36	2291	2296	2301	2307	2312	2317	2323	2328	2333	2339
37	2344	2350	2356	2361	2366	2371	2377	2382	2388	2393
38	2399	2404	2410	2416	2421	2427	2432	2438	2443	2449
39	2455	2460	2466	2472	2477	2483	2488	2494	2499	2505
40	2511	2516	2522	2528	2533	2539	2544	2550	2555	2561
41	2567	2572	2578	2584	2590	2595	2600	2606	2612	2618
42	2624	2630	2636	2642	2648	2654	2660	2665	2671	2677
43	2683	2689	2696	2702	2708	2714	2720	2726	2732	2738
44	2744	2751	2757	2763	2770	2776	2782	2789	2795	2802
45	2808	2815	2822	2828	2835	2842	2848	2855	2862	2868
46	2875	2881	2888	2895	2902	2909	2916	2923	2930	2937
47	2944	2951	2958	2965	2972	2979	2986	2993	3000	3007
48	3014	3021	3028	3035	3042	3049	3056	3063	3070	3078
49	3085	3092	3099	3106	3112	3119	3126	3133	3140	3148

Main Differences





## ANTILOGARITHMS

	0	1	2	3	4	5	6	7	8	9	Mean Differences								
											1	2	3	4	5	6	7	8	9
.50	3162	3170	3177	3184	3192	3199	3206	3214	3221	3228	1	1	2	3	4	4	5	6	7
.51	3236	3243	3251	3259	3266	3273	3281	3289	3296	3304	1	2	2	3	4	5	5	6	7
.52	3311	3319	3327	3334	3342	3350	3357	3366	3373	3381	1	2	2	3	4	5	5	6	7
.53	3388	3396	3404	3412	3420	3428	3436	3443	3451	3459	1	2	2	3	4	5	5	6	7
.54	3467	3475	3483	3491	3499	3506	3515	3524	3532	3540	1	2	2	3	4	5	5	6	7
.55	3548	3556	3565	3573	3581	3589	3597	3606	3614	3622	1	2	2	3	4	5	5	6	7
.56	3631	3639	3648	3656	3664	3673	3681	3690	3698	3707	1	2	3	3	4	5	5	6	7
.57	3715	3724	3733	3741	3750	3758	3767	3776	3784	3793	1	2	3	3	4	5	5	6	7
.58	3802	3811	3819	3828	3837	3846	3855	3864	3873	3882	1	2	3	4	4	5	5	6	7
.59	3890	3899	3908	3917	3926	3936	3945	3954	3963	3972	1	2	3	4	5	5	6	7	8
.60	3981	3990	3999	4009	4018	4027	4036	4046	4055	4064	1	2	3	4	5	6	6	7	8
.61	4074	4083	4093	4102	4111	4121	4130	4140	4150	4159	1	2	3	4	5	6	7	8	9
.62	4169	4178	4188	4198	4207	4217	4227	4236	4246	4256	1	2	3	4	5	6	7	8	9
.63	4266	4276	4285	4295	4305	4315	4325	4335	4345	4355	1	2	3	4	5	6	7	8	9
.64	4365	4375	4385	4395	4406	4416	4426	4436	4446	4457	1	2	3	4	5	6	7	8	9
.65	4467	4477	4487	4498	4508	4519	4529	4539	4550	4560	1	2	3	4	5	6	7	8	9
.66	4571	4581	4592	4603	4613	4624	4634	4645	4656	4667	1	2	3	4	5	6	7	9	10
.67	4677	4688	4699	4710	4721	4732	4742	4753	4764	4775	1	2	3	4	5	7	8	9	10
.68	4786	4797	4808	4819	4831	4842	4853	4864	4875	4887	1	2	3	4	6	7	8	9	10
.69	4898	4909	4920	4932	4943	4955	4966	4977	4989	5000	1	2	3	5	6	7	8	9	10
.70	5012	5023	5035	5047	5058	5070	5082	5093	5105	5117	1	2	4	5	6	7	8	9	11
.71	5129	5140	5152	5164	5176	5188	5200	5212	5224	5236	1	2	4	5	6	7	8	10	11
.72	5248	5260	5272	5284	5297	5309	5321	5333	5346	5358	1	2	4	5	6	7	9	10	11
.73	5370	5383	5396	5408	5420	5433	5446	5458	5470	5483	1	3	4	5	6	8	9	10	11
.74	5495	5508	5521	5534	5546	5559	5572	5585	5598	5610	1	3	4	5	6	8	9	10	12
.75	5623	5636	5649	5662	5675	5689	5702	5715	5728	5741	1	3	4	5	7	8	9	10	12
.76	5754	5768	5781	5794	5808	5821	5834	5848	5861	5875	1	3	4	5	7	8	9	11	12
.77	5888	5902	5916	5929	5943	5957	5970	5984	5998	6012	1	3	4	5	7	8	10	11	12
.78	6026	6039	6053	6067	6081	6095	6109	6124	6138	6152	1	3	4	6	7	8	10	11	13
.79	6166	6180	6194	6209	6223	6237	6252	6266	6281	6295	1	3	4	6	7	9	10	11	13
.80	6310	6324	6339	6353	6368	6383	6397	6412	6427	6442	1	3	4	6	7	9	10	12	13
.81	6457	6471	6486	6501	6516	6531	6546	6561	6577	6592	2	3	5	6	8	9	11	12	14
.82	6607	6622	6637	6653	6668	6683	6699	6714	6730	6745	2	3	5	6	8	9	11	12	14
.83	6761	6776	6792	6808	6823	6839	6855	6871	6887	6902	2	3	5	6	8	9	11	13	14
.84	6918	6934	6950	6966	6982	6998	7015	7031	7047	7063	2	3	5	6	8	10	11	13	15
.85	7079	7096	7112	7129	7146	7161	7178	7194	7211	7228	2	3	5	7	8	10	12	13	15
.86	7244	7261	7278	7295	7311	7328	7345	7362	7379	7396	2	3	6	7	8	10	12	13	15
.87	7413	7430	7447	7464	7482	7499	7518	7534	7551	7568	2	3	6	7	9	10	12	14	16
.88	7586	7603	7621	7638	7656	7674	7691	7709	7727	7745	2	4	6	7	9	11	12	14	16
.89	7762	7780	7798	7816	7834	7852	7870	7889	7907	7925	2	4	6	7	9	11	13	14	16
.90	7943	7962	7980	7998	8017	8035	8054	8072	8091	8110	2	4	6	7	9	11	13	15	17
.91	8128	8147	8166	8185	8204	8222	8241	8260	8279	8299	2	4	6	8	9	11	13	15	17
.92	8318	8337	8356	8375	8395	8414	8433	8453	8472	8492	2	4	6	8	10	12	14	15	17
.93	8511	8531	8551	8570	8590	8610	8630	8650	8670	8690	2	4	6	8	10	12	14	16	18
.94	8710	8730	8750	8770	8790	8810	8831	8851	8872	8892	2	4	6	8	10	12	14	16	18
.95	8913	8933	8954	8974	8995	9016	9036	9057	9078	9099	2	4	6	8	10	12	15	17	19
.96	9120	9141	9162	9183	9204	9226	9247	9268	9290	9311	2	4	6	8	11	13	15	17	19
.97	9333	9354	9376	9397	9419	9441	9463	9484	9506	9528	2	4	7	9	11	13	16	17	20
.98	9550	9572	9594	9616	9638	9661	9683	9705	9727	9750	2	4	7	9	11	13	16	18	20
.99	9772	9795	9817	9840	9863	9886	9908	9931	9954	9977	2	5	7	9	11	14	16	18	20



## PHYSICAL SCIENCES

### Paper - II

1. A periodic function  $f(t)$  is defined in the interval  $(-\pi, \pi)$  as

$$f(t) = \begin{cases} 0 & -\pi < t < 0 \\ 2V_0 & 0 < t < \pi \end{cases}$$

Fourier coefficients ( $a_n$  and  $b_n$  for sine and cosine parts) of the Fourier series of the signal are

- (A)  $a_n = 0, b_n = 0$  for even 'n',  $b_n = \frac{4V_0}{n\pi}$  for odd 'n'
- (B)  $a_n = 0, b_n = \frac{4V_0}{n\pi}$  for even 'n',  $b_n = 0$  for odd 'n'
- (C)  $a_0 = 2V_0, a_n = 0$  (for  $n > 0$ ),  $b_n = 0$  for even 'n',  $b_n = \frac{4V_0}{n\pi}$  for odd 'n'
- (D)  $a_0 = 2V_0, a_n = 0$  ( $n > 0$ ),  $b_n = \frac{4V_0}{n\pi}$  for even 'n',  $b_n = 0$  for odd 'n'
2. A coin toss experiment is conducted using a biased coin with only 30% chance of returning 'head'. The probability of getting exactly 2 heads in 5 trials of the experiment is
- (A) 13% (B) 21%
- (C) 31% (D) 44%
3. Consider a function  $f(z) = 2z^3 - 3iz^2 + 4$ , where  $z$  is a complex variable. Which of the following statements is TRUE ?
- (A)  $f(z)$  is holomorphic everywhere in the complex plane
- (B)  $f(z)$  is not holomorphic
- (C)  $f(z)$  is holomorphic in some regions of the complex plane
- (D)  $f(z)$  is holomorphic only near  $z = 0$  but not elsewhere
4. Matrix  $A = \begin{bmatrix} 2 & 1 \\ 3 & 4 \end{bmatrix}$ , then  $4m^2 - 6m + 5I$  (where  $I$  is the identity matrix) is
- (A)  $m^2$
- (B)  $3m^2$
- (C)  $m^2 - 6m + 5I$
- (D)  $3m^2 - 6m + 5I$



5. The value of the integral  $G(F) = -\int_{-\infty}^{\infty} \delta(x) e^{i2\pi fx} dx$  where  $\delta(x)$  is the Dirac delta is
- (A)  $G(F) = 0$
  - (B)  $G(F) = 1$
  - (C)  $G(F) = F$
  - (D)  $G(F) = 2\pi F$
6. A complex number satisfies the condition  $z^2 + 2z + 1 = 0$ , then the value of  $Z$  for which the real and imaginary parts are non-zero is,
- (A)  $z = -1 + 1i$
  - (B)  $z = -1 + 2i$
  - (C)  $z = 2 + 1i$
  - (D)  $z = 1 + 2i$
7. Second term in the Taylor series expansion of  $\frac{n^2 - 1}{n^2 + 2n + 1}$  around 0 is
- (A) 1
  - (B)  $n$
  - (C)  $2n$
  - (D)  $-n^2$
8. Bisection method is used to estimate the roots of  $n^2 - 4 = 0$  with initial values of  $a = 0$  and  $b = 6$  (points between which the root is to be estimated). The value of the estimated root after 5 iterations of the method is
- (A) 1.52
  - (B) 1.875
  - (C) 2.062
  - (D) 2.250
9. The residue of the function  $f(z) = \frac{4z^2}{(z^{11} + 2)(z - 1)}$  for a simple pole at  $z = 1$  is
- (A) 0
  - (B)  $\frac{3}{4}$
  - (C) 1
  - (D)  $\frac{4}{3}$





10. Value of third order (  $n = 3$  ) Laguerre polynomial  $L_3(n)$  at  $n = 1$  is
- (A)  $-\frac{2}{3}$
  - (B)  $\frac{2}{3}$
  - (C)  $-\frac{3}{2}$
  - (D)  $\frac{3}{2}$
11. Which of the following is true for a covariant tensor ?
- (A) It transforms using inverse of the Jacobian matrix
  - (B) It transforms using the Jacobian matrix
  - (C) It does not transform under coordinate changes
  - (D) It transforms as a covariant vector
12. In electrical circuits, the Laplace transform is used to analyze the circuit's behavior. If  $V(s)$  is the Laplace transform of the time varying voltage what does the variable 's' represent ?
- (A) Frequency of the voltage source
  - (B) Complex frequency, including to the decay and oscillation
  - (C) Time variation of frequency
  - (D) Resistance in the circuit
13. The Coriolis effect is most noticeable
- (A) At poles of the earth
  - (B) At the equator
  - (C) At mid-latitudes
  - (D) Everywhere on earth equally



14. A particle of mass  $m$  moves under the influence of the potential  $V(n) = \frac{A}{n^2} - \frac{B}{n}$ , where the constants  $A, B > 0$ . The frequency  $\omega$  of small oscillations around the equilibrium point will be

(A)  $\sqrt{\frac{2A}{mB}}$

(B)  $\sqrt{\frac{2B}{mA}}$

(C)  $\sqrt{\frac{B^4}{8mA^3}}$

(D)  $\sqrt{\frac{A^4}{8mB^3}}$

15. The lagrangian ( $L$ ) for a particle of mass ' $m$ ' moving in a central force field is given by  $L = \frac{m}{2}(\dot{r}^2 + r^2 \dot{\theta}^2) + \frac{k}{r}$ , which of the following represents a conserved quantity ?

(A)  $mr^2\dot{\theta}$

(B)  $mr\dot{\theta}^2 - \frac{k}{r^2}$

(C)  $mr^2\dot{\theta}^2$

(D)  $mr$

16. Consider two masses  $m_1$  and  $m_2$  connected by three springs with spring constants  $K_1, K_2$  and  $K_3$ , where the masses are free to move in one dimension.



The number of generalized coordinate for the description of motion are

(A) 1

(B) 2

(C) 3

(D) 4



17. For a rigid body, the diagonal components of the moment of inertia tensor represent
- (A) Products of inertia
  - (B) Principal moments of inertia
  - (C) Mass of the body
  - (D) Angular momentum
18. In a two body collision problem of two masses  $m_1$  and  $m_2$  moving with velocities  $v_1$  and  $v_2$  respectively, the velocity of the centre of mass is given by
- (A) 0
  - (B)  $\frac{(m_1 v_1 + m_2 v_2)}{(m_1 + m_2)}$
  - (C)  $\frac{(v_1 + v_2)}{2}$
  - (D)  $\frac{(m_1 v_2 + m_2 v_1)}{(m_1 + m_2)}$
19. A rigid rod of negligible thickness has  $N$  rotational degrees of freedom in a 3-space coordinate system. Then  $N$  equals to
- (A) 1
  - (B) 2
  - (C) 3
  - (D) 4
20. A two dimensional dynamical system is governed by the Lagrangian  $L = k^2 (\dot{x}^2 + \dot{y}^2) - m^2(x + y)^2$ . The Hamiltonian in this case becomes
- (A)  $m^2(\dot{x}^2 + \dot{y}^2) + k^2(x + y)^2$
  - (B)  $2k^2(\dot{x}^2 + \dot{y}^2) + m^2(x + y)^2$
  - (C)  $2k^2(\dot{x}^2 + \dot{y}^2) + m^2(x^2 + y^2)$
  - (D)  $m^2(x + y)^2 + k^2(\dot{x}^2 + \dot{y}^2)$
21. In the recent SOLAR mission by ISRO, Aditya L1 is believed to move in a “halo” orbit around an axis connecting the SUN and the EARTH. Select the correct statement from below on the “Halo Orbit”.
- (A) It is an elliptical orbit in 3-space
  - (B) It is an elliptical orbit in 2-space
  - (C) It is a circular orbit in 2-space
  - (D) It is a circular orbit in 3-space



**22.** The Lagrangian  $L(q_i, \dot{q}_i, t)$  is defined for all cyclic coordinates. Select the correct statement from below.

- (A) The canonical conjugates  $p_i$  to  $q_i$  are conserved
- (B) The canonical conjugates  $p_i$  to  $q_i$  are not conserved
- (C) The energy remains conserved
- (D) The applied force remains conserved

**23.** The time dependent Hamilton-Jacobi equation for a harmonic system described with two degrees of freedom is given by

- (A)  $H\left(q_1, q_2, q_3 \dots q_n, \frac{\partial w}{\partial q_1}, \frac{\partial w}{\partial q_2} \dots\right) + \frac{\partial w}{\partial t} = 0$
- (B)  $H\left(q_1, q_2, q_3 \dots q_n, \frac{dw}{dq_1}, \frac{dw}{dq_2} \dots\right) + \frac{dw}{dt} = 0$
- (C)  $H(q_1, q_2) + \frac{dw}{dt} = 0$
- (D)  $H\left(q_1, q_2, \frac{\partial w}{\partial q_1}, \frac{\partial w}{\partial q_2}\right) + \frac{\partial w}{\partial t} = 0$

**24.** The proper time ( $T$ ) in special theory of relativity is given as

$$dT^2 = (-c^2 dt^2 + dx^2 + dy^2 + dz^2)$$

Select the correct statement from the options below.

- (A)  $dT^2 > 0$  for space-like and  $dT^2 < 0$  for time-like
- (B)  $dT^2 < 0$  for space-like and  $dT^2 > 0$  for time-like
- (C)  $dT^2 < 0$  for space-like and  $dT^2 = 0$  for time-like
- (D)  $dT^2 > 0$  for space-like and  $dT^2 = 0$  for time-like

**25.** Electromagnetic wave of wavelength 532 nm, polarized parallel to the plane of incidence is obliquely incident at an angle of  $49^\circ$  (with respect to the surface normal) at the interface between two non-magnetic dielectric mediums of refractive indices  $n_1 = 1.33$  and  $n_2 = 1.53$  (em radiation travels from medium of  $n_1$  to  $n_2$ ). The percentage of incident light which is reflected is

- (A) 0
- (B) 5
- (C) 7
- (D) 26.4



26. 'N' charged drops each of charge 'q' and radius 'r' coalesce to form a big drop of radius 'R' and charge 'Q'. If V is the electric potential and E is the electric field at the surface of the drop, then

(A)  $E_{\text{big}} = N^{\frac{2}{3}} E_{\text{small}}$

(B)  $V_{\text{big}} = N^{\frac{1}{3}} E_{\text{small}}$

(C)  $E_{\text{small}} = N^{\frac{2}{3}} E_{\text{big}}$

(D)  $V_{\text{big}} = N^{\frac{2}{3}} V_{\text{small}}$

27. A beam of linearly polarized light passes through two polarizers. The first is set at an angle of  $45^\circ$  to the initial polarization direction. The second is set at an angle of  $90^\circ$  to the initial polarization direction. The fraction of light intensity after second polarizer is

(A)  $\frac{1}{4}$

(B)  $\frac{3}{8}$

(C)  $\frac{1}{2}$

(D) 0

28. Consider a uniformly magnetized circular cylinder of radius R with its axis coinciding with the z - axis. The magnetization inside the cylinder is  $\vec{M} = M_0 \hat{z}$ .  $\vec{H}(\vec{r})$  and  $\vec{B}(\vec{r})$  everywhere in space is

(A)  $\vec{H}(\vec{r}) = 0, \vec{B}(\vec{r}) = \mu_0 M_0 \hat{z}$  for  $r < R$

(B)  $\vec{H}(\vec{r}) = 0, \vec{B}(\vec{r}) = 0$  for  $r < R$

(C)  $\vec{H}(\vec{r}) = \mu_0 M_0 \hat{z}, \vec{B}(\vec{r}) = 0$  for  $r < R$

(D)  $\vec{H}(\vec{r}) = M_0 \hat{z}, \vec{B}(\vec{r}) = 0$  for  $r > R$



29. A pair of scalar ( $V$ ) and vector ( $\vec{A}$ ) potentials are given by

$$V(\vec{r}, t) = 0 \quad \vec{A}(\vec{r}, t) = -\frac{1}{4\pi\epsilon_0} \frac{qt}{r^2} \hat{r}$$

Where  $\hat{r}$  is the unit vector along  $\vec{r}$  which of the following is TRUE ?

- (A) The pair of potentials satisfy Coulomb and Lorenz gauge conditions
  - (B) The pair of potentials satisfy Coulomb gauge condition only
  - (C) The pair of potentials satisfy Lorenz gauge condition only
  - (D) The pair of potentials does not satisfy either Coulomb or Lorenz gauge conditions
30. Divergence of Maxwell stress tensor represents
- (A) Net force per unit area
  - (B) Net force per unit volume
  - (C) Net charge per unit area
  - (D) Net charge per unit volume
31. Poynting's theorem states that in a volume containing charges
- (A) Work done on charges by em forces = Decrease in energy remaining in the fields - Energy flown out through the surface
  - (B) Work done on charges by em forces = Decrease in energy remaining in the fields + energy flown out through the surface
  - (C) Work done on the charges by em forces = Decrease in energy remaining in the field
  - (D) Work done on charges by em forces = Energy flown out through the surface
32. A point charge is moving with a speed of  $0.1 C$  ( $C$  is the speed of light in vacuum). It changes its speed to  $0.75 C$ . Ratio of the electric fields of the charge at a point perpendicular to its direction of motion (After and before increase in speed)
- (A) 0
  - (B) 1
  - (C) 1.25
  - (D) 1.5



33. Two linearly polarized plane wave fronts with an angle of  $60^\circ$  between their planes of polarization are superposed. If the intensities of the two beams are  $I_1 = I_0$  and  $I_2 = 0.7 I_0$ . The visibility (or contrast) of the resulting interference fringes is
- (A) 0 (B) 0.25  
(C) 0.5 (D) 1
34. On an average the intensity of sunlight received by earth is  $1380 \text{ W/m}^2$ . The force exerted by sunlight on a perfect reflector of area  $1 \text{ m}^2$  kept normal to it (on the surface of the earth) is
- (A)  $0 \sim \text{N}$  (B)  $4P \sim \text{N}$   
(C)  $92 \sim \text{N}$  (D)  $184 \sim \text{N}$
35. The power radiated by a single hydrogen atom, considering it an electric dipole (electron and proton are separated by a distance equal to one Bohr radius) with electric dipole moment of  $10 \times 10^{-30} \text{ cm}$ , when subjected to a field oscillating at frequency  $\delta = 10^{15} \text{ Hz}$  is
- (A)  $1.1 \times 10^{-14} \text{ W}$  (B)  $7 \times 10^{-14} \text{ W}$   
(C)  $5.3 \times 10^{-12} \text{ W}$  (D)  $1.7 \times 10^{-11} \text{ W}$
36. Electron number density ( $n$ ) of a laser induced lead-calcium plasma is  $10^{23}/\text{m}^3$ . The cut-off frequency ( $\gamma_{\text{cut-off}}$ ) for this plasma is [given  $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$ ,  $m_e = 9.1 \times 10^{-31} \text{ kg}$ ,  $e = 1.602 \times 10^{-19} \text{ C}$ ]
- (A)  $0.36 \times 10^{11} \text{ Hz}$  (B)  $0.71 \times 10^{12} \text{ Hz}$   
(C)  $1.43 \times 10^{12} \text{ Hz}$  (D)  $2.85 \times 10^{12} \text{ Hz}$
37. A subatomic particle produced in a nuclear collision is found to have a mass such that  $mc^2 = 1228 \text{ MeV}$ , with an uncertainty of  $\pm 56 \text{ MeV}$ . If it travels with a speed of  $10^8 \text{ m/s}$  after being produced, how far can it travel before it disintegrates ?
- (A)  $1.72 \times 10^{-6} \text{ m}$  (B)  $3.51 \times 10^{-9} \text{ m}$   
(C)  $4.81 \times 10^{-12} \text{ m}$  (D)  $5.86 \times 10^{-16} \text{ m}$



38. An electron moves in a one dimensional potential well of width  $8 \text{ \AA}$  and depth  $12 \text{ eV}$ . Find the number of bound states present.
- (A) 3 (B) 4  
(C) 5 (D) 6
39. A pair of virtual particles is created for a short time. During the time of their existence a distance of  $0.35 \text{ fm}$  is covered with a speed very close to the speed of light. What is the value of  $mc^2$  for each of the virtual particle ?
- (A)  $243.31 \text{ KeV}$   
(B)  $12.52 \text{ MeV}$   
(C)  $140.56 \text{ MeV}$   
(D)  $281.12 \text{ MeV}$
40. An electron in the  $n = 2$  state of hydrogen remains there on the average time of about  $10^{-8} \text{ s}$  before making a transition to  $n = 1$  state. Estimate the width of this line in the spectrum of hydrogen atom.
- (A)  $3.93 \times 10^{-7} \text{ nm}$   
(B)  $1.32 \times 10^{-9} \text{ nm}$   
(C)  $2.74 \times 10^{-2} \text{ nm}$   
(D)  $5.41 \times 10^{-3} \text{ nm}$
41. The expectation value of x component of spin angular momentum of a fermion in state  $\begin{pmatrix} 2 \\ 1-i \end{pmatrix}$
- (A)  $2\hbar$  (B)  $\hbar/2$   
(C)  $\hbar$  (D)  $3\hbar/2$





42. The Hamiltonian of a two-electron system is perturbed by an interaction  $\alpha S_1 \cdot S_2$ , where  $\alpha$  is a constant and  $S_1$  and  $S_2$  are spin angular momenta of electrons. Calculate the splitting between the  $S = 0$  and  $S = 1$  states by first order perturbation where  $S$  is the total magnitude of the total spin.

- (A)  $\alpha \hbar^2/4$  (B)  $2 \alpha \hbar^2$   
(C)  $\alpha \hbar^2$  (D)  $\alpha \hbar$

43. Estimate the kinetic energy of the particle trapped in a delta function potential

$$H = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} - \alpha \delta(x) \text{ using a Gaussian trial wave function } \psi(x) = Ae^{-bx^2}.$$

- (A)  $\frac{\hbar b^2}{4m}$  (B)  $\frac{\hbar^2 b}{2m}$   
(C)  $\frac{\hbar^2 b^2}{2m}$  (D)  $\frac{\hbar^2 b^2}{4m^2}$

44. A particle of mass  $m$  is confined in the potential

$$V(x) = \begin{cases} \frac{1}{2} m\omega^2 x^2 & \text{for } x > 0 \\ \alpha & \text{for } x \leq 0 \end{cases}$$

Let the wave function of the particle is

$$\psi(x) = -\frac{1}{\sqrt{5}} \psi_0 + \frac{2}{\sqrt{5}} \psi_1$$

Where  $\psi_0$  and  $\psi_1$  are eigen functions of the ground state and the first excited states, respectively. The expectation value of the energy is

- (A)  $\frac{31}{10} \hbar\omega$  (B)  $\frac{11}{10} \hbar\omega$   
(C)  $\frac{13}{10} \hbar\omega$  (D)  $\frac{25}{10} \hbar\omega$

45. The recoil momentum of an atom is  $P_A$  when it emits an infrared photon of wavelength 1500 nm, and it is  $P_B$  when it emits a photon of visible wavelength 500 nm. The ratio of  $\frac{P_A}{P_B}$  is

- (A) 1 : 1 (B)  $1 : \sqrt{3}$  (C) 1 : 3 (D) 3 : 1



46. If  $x$  and  $p$  are the  $x$  components of the position and momentum operators of a particle, respectively, the commutator  $[x^2, p^2]$  is

(A)  $i\hbar (xp - px)$  (B)  $2i\hbar (xp - px)$

(C)  $i\hbar (xp + px)$  (D)  $2i\hbar (px + xp)$

47. If  $\bar{S}_1$  and  $\bar{S}_2$  are the spin operators of the two electrons of a Helium atom, the value of  $\langle \bar{S}_1 \cdot \bar{S}_2 \rangle$  for the ground state is

(A)  $-\frac{3}{2}\hbar^2$  (B)  $-\frac{3}{4}\hbar^2$  (C) 0 (D)  $\frac{3}{2}\hbar^2$

48. The scattering of particles by a potential can be analyzed by Born approximation. In particular, if the scattered wave is replaced by an appropriate plane wave, the corresponding Born approximation is known as the first Born approximation, such an approximation is valid for

(A) Large incident energies and weak scattering potentials

(B) Large incident energies and strong scattering potentials

(C) Small incident energies and weak scattering potentials

(D) Small incident energies and strong scattering potentials

49. For a system of 'N' independent, quantum harmonic oscillators, the canonical partition function is given by

$$Z = \frac{\exp\left(\frac{-N\beta\hbar\omega}{2}\right)}{1 - \exp(-\beta\hbar\omega)^N}$$

The internal energy of the system will be

(A)  $U = N \left[ \frac{\hbar\omega}{2} + \frac{\hbar\omega}{\exp(\beta\hbar\omega) - 1} \right]$  (B)  $U = N \left[ \frac{\hbar\omega}{2} + \frac{\hbar\omega}{1 - \exp(-\beta\hbar\omega)} \right]$

(C)  $U = N \left[ \frac{\hbar\omega}{2} + \frac{\hbar\omega \exp\left(\frac{-N\beta\hbar\omega}{2}\right)}{1 - \exp(-\beta\hbar\omega)} \right]$  (D)  $U = N \left[ \frac{\hbar\omega}{2} + \frac{\exp\left(\frac{-N\beta\hbar\omega}{2}\right)}{\exp(\beta\hbar\omega) - 1} \right]$



50. Consider a system with two energy levels  $E_0 = 0$  and  $E_1 = \epsilon$ . The system is in contact with a heat reservoir at temperature  $T$ . With a parameter defined as

$\beta = \frac{1}{kT}$ , the canonical partition function of the system will be

- (A)  $e^{-\beta\epsilon}$  (B)  $e^{\beta\epsilon}$   
(C)  $1 + e^{-\beta\epsilon}$  (D)  $1 - e^{-\beta\epsilon}$

51. Identify the correct statement.

- (A) The entropy of a system always increases when it undergoes an irreversible process  
(B) The entropy of a system always decreases when it undergoes an irreversible process  
(C) The second law of thermodynamics follow directly from the principle of the conservation of energy  
(D) The internal energy of an ideal gas do not depend on temperature

52. If the number density of a free electron gas in three dimension is increased eight times, its fermi temperature will

- (A) Increase by a factor of 4 (B) Decrease by a factor of 4  
(C) Increase by a factor of 8 (D) Decrease by a factor of 8

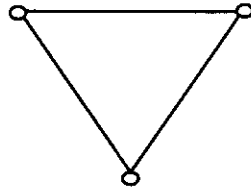
53. The Helmholtz free energy ( $F$ ) for a system of 'N' independent harmonic oscillators in a canonical ensemble is given by

$F = N kT \ln \left( \frac{\hbar \omega}{kT} \right)$ . What will be the entropy of the system [ $k$  - Boltzmann constant,  $T$  - temperature and other symbols have their usual physical meaning ] ?

- (A)  $S = kT \ln \left( \frac{\hbar \omega}{kT} \right)$   
(B)  $S = Nk \ln \left( \frac{\hbar \omega}{kT} \right)$   
(C)  $S = Nk \left[ \ln \left( \frac{kT}{\hbar \omega} \right) + 1 \right]$   
(D)  $S = Nk \left[ \ln \left( \frac{\hbar \omega}{kT} \right) + 1 \right]$



54. Consider a triatomic molecule of the shape shown in the figure below in 3 dimensions. The heat capacity of this molecule at high temperature is  
[Temperature much higher than the vibrational and rotational energy scales of the molecule but lower than its bond dislocation energies]



- (A)  $\frac{3}{2} k_B$       (B)  $3 k_B$       (C)  $\frac{9}{2} k_B$       (D)  $6 k_B$
55. Consider two independent systems of identical particles. The mass of the particles in system 1 and system 2 are  $m_1$  and  $m_2$ , respectively. Also  $m_2 = 4m_1$ . If the densities of these particles ( $m_1$  and  $m_2$ ) at a given temperature are equal, which of the following are true for the mean thermal wavelengths for the particles in the two systems ?
- (A)  $\lambda_1 = \lambda_2$       (B)  $\lambda_1 = 4\lambda_2$   
(C)  $\lambda_1 = \lambda_2/2$       (D)  $\lambda_1 = 2\lambda_2$
56. The maximum value of fugacity of an ideal Bose gas is
- (A)  $1/2$       (B)  $1$   
(C)  $3/2$       (D)  $\infty$
57. The correct range for values of fugacity of an ideal Fermi gas system is
- (A)  $0 \leq z \leq \infty$       (B)  $1/2 \leq z \leq \infty$   
(C)  $0 \leq z \leq 1$       (D)  $1/2 \leq z \leq 1$
58. Partition function for a gas of photons is given as  $\ln z = \frac{\pi^2 v (k_B T)^3}{45 \hbar^3 C^3}$ .  
The specific heat of the photon gas varies with temperature as
- (A)  $C \propto T^{1/3}$       (B)  $C \propto T^2$   
(C)  $C \propto T^3$       (D)  $C \propto T^{2/3}$



59. Consider a system of  $N$  atoms of an ideal gas of type A at temperature  $T$  and volume  $V$ . It is kept in diffusive contact with another system of  $N$  atoms of another ideal gas type B at the same temperature  $T$  and volume  $V$ . Once the combined system reaches equilibrium

- (A) The total entropy of the final system is the same as the sum of the entropies of the individual systems
- (B) The entropy of mixing is  $2 N k_B \ln 2$
- (C) The entropy of the final system is less than that of sum of the entropies of the two gases
- (D) The entropy of the mixing is non zero when the atoms A and B are of the same type

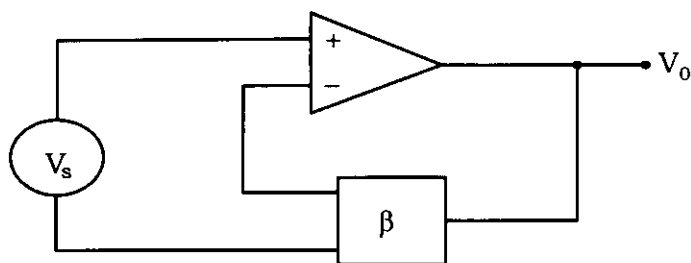
60. In a thermodynamic system in equilibrium, each molecule can exist in three possible states with the probabilities  $\frac{1}{2}$ ,  $\frac{1}{3}$  and  $\frac{1}{6}$ , respectively. The entropy per molecule is

- (A)  $\frac{1}{2} k_B \ln 3 + \frac{2}{3} k_B \ln 2$
- (B)  $\frac{1}{2} k_B \ln 2 + \frac{1}{6} k_B \ln 3$
- (C)  $\frac{1}{2} k_B \ln 2 + \frac{2}{3} k_B \ln 3$
- (D)  $\frac{1}{2} k_B \ln 3$

61. Which of the following does NOT pertain to digital systems ?

- (A) Binary numbers
- (B) Calculus of differences
- (C) Quadrature shift keying
- (D) Second order differential equations

62. Find out the differential input voltage ( $V_{id}$ ) in the negative feedback amplifier shown below. Given  $A_v = -500$ ,  $\beta = -0.1$  and  $V_s = 0.1$  V.

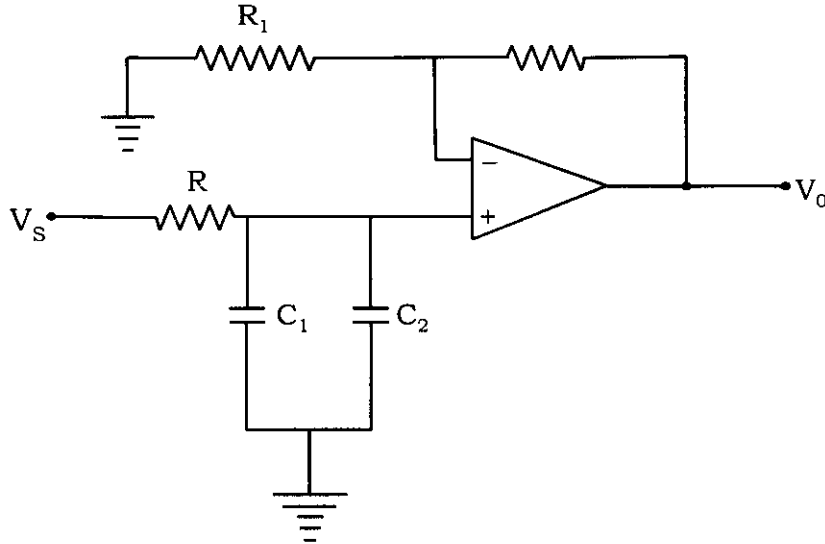


- (A) 0.001 V
- (B) 0.01 V
- (C) 0.002 V
- (D) 0.02 V



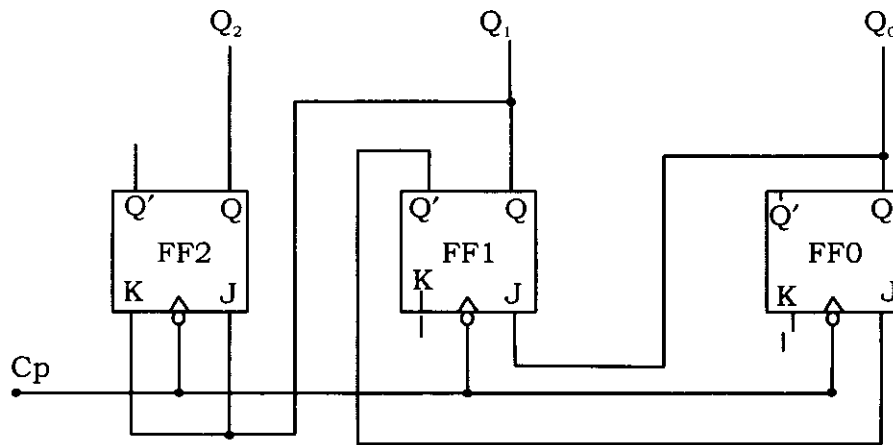
63. Which of the following is analog communication ?
- (A) Quadrature phase shift keying method
  - (B) Medium wave radio communication
  - (C) Pulse amplitude modulation method
  - (D) Frequency shift keying method

64. The network shown below is a



- (A) High pass active filter
- (B) Band pass active filter
- (C) Band reject active filter
- (D) Low pass active filter

65. The missing counts in the binary irregular counter shown below are



- (A) 100 and 101
- (B) 011 and 111
- (C) 100 and 110
- (D) 010 and 101



66. Find out which of the following is more versatile.
- (A) OR
  - (B) NOR
  - (C) XOR
  - (D) AND
67. Thermocouples are
- (A) Passive transducers
  - (B) Active transducers
  - (C) Both active and passive transducers
  - (D) Output transducers
68. A solar cell has an open circuit voltage ( $V_{OC}$ ) of 0.6 V and short circuit current ( $I_{SC}$ ) of 2.5 A and fill factor of 0.7. If the incident power of light on the solar cell is 20 W, its efficiency is
- (A) 2.25%
  - (B) 5.25%
  - (C) 10.71%
  - (D) 14.32%
69. A silicon photodiode has a responsivity of 0.67 A/W at 850 nm. If light of 850 nm is incident on the photodiode and the measured photocurrent is 0.0134 mA, the power of the incident light is
- (A) 10 mW
  - (B) 20 mW
  - (C) 40 mW
  - (D) 80 mW
70. The target of X-ray tube is subjected to excitation voltage  $V$ . The wavelength of the excited X-rays is proportional to
- (A)  $\frac{1}{\sqrt{V}}$
  - (B)  $V$
  - (C)  $\frac{1}{V}$
  - (D)  $\sqrt{V}$



71. The emission wavelength for the transition  ${}^1D_2 \rightarrow {}^1F_3$  is  $3122 \text{ \AA}$ . The ratio of population of the final states at a temperature  $5000 \text{ K}$  is ( $h = 6.626 \times 10^{-34} \text{ J s}$ ,  $k_B = 1.380 \times 10^{-23} \text{ J K}$ )
- (A)  $4.02 \times 10^{-5}$
  - (B)  $2.03 \times 10^{-5}$
  - (C)  $9.83 \times 10^{-5}$
  - (D)  $7.02 \times 10^{-5}$
72. The hyperfine structure of  $\text{Na}(3 {}^2P_{3/2})$  with nuclear spin  $I = 3/2$  has
- (A) 1 state
  - (B) 2 states
  - (C) 3 states
  - (D) 4 states
73. Light of wavelength  $1.5 \text{ \mu m}$  incident on a material with a characteristic Raman frequency of  $20 \times 10^{12} \text{ Hz}$  results in a Stokes shifted line of wavelength
- (A)  $1.47 \text{ \mu m}$
  - (B)  $1.57 \text{ \mu m}$
  - (C)  $1.67 \text{ \mu m}$
  - (D)  $1.77 \text{ \mu m}$
74. In a laser system transition occurs from higher energy band  $E_2$  to lower energy band  $E_1$ . If the energy widths of the higher and lower levels ( $\Delta E_2$  and  $\Delta E_1$ ) are  $0.01 \text{ eV}$  and  $0.0025 \text{ eV}$  respectively the coherence length of the emitted laser line is
- (A)  $0.1 \text{ mm}$
  - (B)  $1 \text{ mm}$
  - (C)  $1 \text{ cm}$
  - (D)  $1 \text{ m}$





75. A sample shows an ESR signal at magnetic field 0.2 T and frequency 5.6 GHz. The  $f$  - factor of the sample is [Given  $\mu_B$  (Bohr Magnetron) -  $9.274 \times 10^{-24}$  J/T]
- (A) 1.8
  - (B) 1.9
  - (C) 2.0
  - (D) 2.1
76. An atom with polarizability  $\alpha = 2.5 \times 10^{-29} \text{ m}^3$  is placed in an external electric field of  $10^5 \text{ V/m}$ . Calculate the energy shift due to quadratic stark effect.
- (A) 0.39 eV
  - (B) 0.78 eV
  - (C) 1.56 eV
  - (D) 3.12 eV
77. Is the reaction  $P\bar{P} \rightarrow \pi^+ \pi^-$  allowed
- (A) Yes
  - (B) No
  - (C) Allowed only under weak interaction
  - (D) Allowed only under electromagnetic interaction
78. According to liquid drop model, the binding energy per nucleon
- (A) Increases with increasing mass number for all nuclei
  - (B) Decreases with increasing mass number for all nuclei
  - (C) Remains same with increasing mass number
  - (D) Increases with mass number and then decreases slowly
79. Which of the following particles has hyper charge  $Y = 0$  ?
- (A) Proton
  - (B) Neutron
  - (C) Pion
  - (D) Kaon



- 80.** What is the weak isospin quantum number of a left-handed electron neutrino ?  
(A) 0 (B)  $+\frac{1}{2}$   
(C)  $-\frac{1}{2}$  (D) 1
- 81.** What is the quark content of  $\Sigma^+$  baryon ?  
(A) uds  
(B) dds  
(C) uus  
(D) uss
- 82.** A nuclear reactor produces 100 MW of power by fission of Uranium - 235. If each fission releases 200 MeV how many Uranium atoms must undergo fission per second to produce this power ?  
(A)  $3.125 \times 10^{18}$   
(B)  $6.25 \times 10^{18}$   
(C)  $12.50 \times 10^{18}$   
(D)  $25.0 \times 10^{18}$
- 83.** Among all four fundamental forces in nature (gravitational, electromagnetic, weak and strong), the long range force is  
(A) Weak and electromagnetic  
(B) Electromagnetic and gravitational  
(C) Weak and strong  
(D) Strong and gravitational
- 84.** The deuteron has a magnetic moment of  $0.857 \mu\text{N}$ . What does this suggest about the contributions from the proton and neutron ?  
(A) Only proton contributes to magnetic moment  
(B) Only neutron contributes to the magnetic moment  
(C) Both proton and neutron contribute, but proton's contribution is dominant  
(D) Both proton and neutron contribute, but neutrons contribution is dominant



85. For a nucleus exhibiting rotational spectra the energy levels are given by

$E_J = \frac{\hbar^2}{2I} J(J+1)$ . If the moment of inertia (I) is  $3 \times 10^{-47} \text{kgm}^2$ , what is the energy of the first excited rotational state ?

- (A) 0.11 MeV
- (B) 0.22 MeV
- (C) 0.44 MeV
- (D) 0.88 MeV

86. The primary reason for the short-range nature of nuclear force is

- (A) Exchange of virtual photons
- (B) Exchange of pions
- (C) Exchange of gluons
- (D) Exchange of W and Z bosons

87. In the nuclear shell model, what is the primary reason for occurrence of magic numbers ?

- (A) Spin-orbit coupling
- (B) Pauli exclusion principle
- (C) Coulomb repulsion
- (D) Nuclear deformation

88. Determine the spin parity of  $^{41}_{20}\text{Ca}$  nucleus in its ground state.

- (A)  $\left(\frac{3}{2}\right)^+$
- (B)  $\left(\frac{5}{2}\right)^-$
- (C)  $\left(\frac{7}{2}\right)^-$
- (D)  $\left(\frac{9}{2}\right)^+$

89. In superconducting state

- (A) Entropy increases and thermal conductivity decreases
- (B) Entropy and thermal conductivity decreases
- (C) Entropy and thermal conductivity increases
- (D) Entropy decreases and thermal conductivity increases



90. The relation gives the potential energy of a diatomic molecule

(A)  $-\frac{a}{r^m} + \frac{b}{r^n}$

(B)  $\frac{a}{r^m} - \frac{b}{r^n}$

(C)  $ar^m + br^n$

(D)  $ar^m - br^n$

91. The equilibrium concentration of a Frenkel defect in crystals is given by

(A)  $n_f = N \exp\left[-\frac{E_f}{KT}\right]$

(B)  $n_f = NN' \exp\left[-\frac{E_f}{KT}\right]$

(C)  $n_f = NN' \exp\left[-\frac{E_f}{2KT}\right]$

(D)  $n_f = NN' \exp\left[-\frac{2E_f}{KT}\right]$

92. The dispersion relation for electrons in the conduction band of a semiconductor is given by  $E = E_0 + \alpha k^2$ , where  $\alpha$  and  $E_0$  are constants. If  $\omega_c$  is the cyclotron frequency of the conduction band electrons in magnetic field  $\bar{B}$ , calculate the value of  $\alpha$ .

(A)  $\frac{\hbar^2 \omega_c}{2e\bar{B}}$

(B)  $\frac{\hbar^2 \omega_c}{4e\bar{B}}$

(C)  $\frac{\hbar^2 \omega_c}{e\bar{B}}$

(D)  $\frac{2\hbar^2 \omega_c}{e\bar{B}}$

93. The crystal structure is NOT studied through the diffraction of

(A) Electron

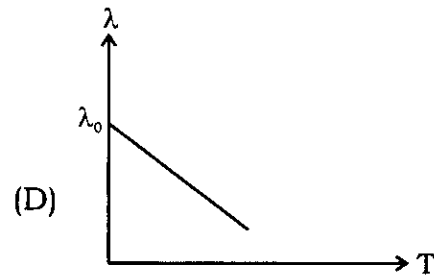
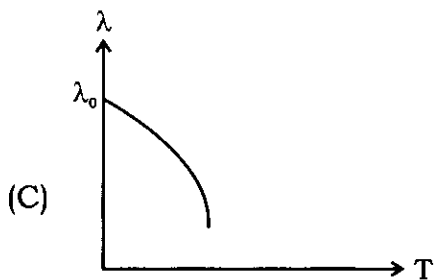
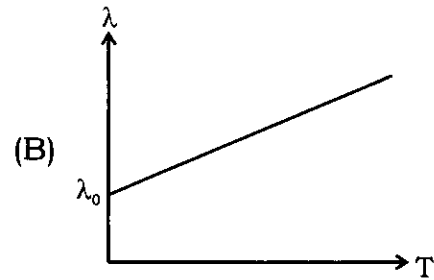
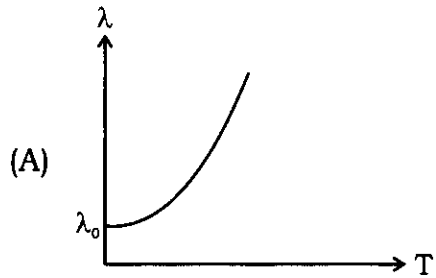
(B) Proton

(C) Neutron

(D) X-rays



94. The graph between penetration depth ( $\lambda$ ) and temperature ( $T$ ) is given by



95. At low temperatures ( $T$ ), the specific heat of common metals is described by ( $\alpha$  and  $\beta$  are constants)

- (A)  $\beta T^3$
- (B)  $\alpha T + \beta T^3$
- (C)  $\alpha T^2 + \beta T^3$
- (D)  $\alpha T^3 + \beta T$

96. In order to estimate the specific heat of phonons, the appropriate method to apply would be

- (A) Einstein model for acoustical phonons and Debye model for optical phonons
- (B) Einstein model for optical phonons and Debye model for acoustical phonons
- (C) Einstein model for both optical and acoustical phonons
- (D) Debye model for both optical and acoustical phonons



97. The maximum allowed frequency  $(\omega_f)_{\max}$  for optical branch in one dimensional diatomic lattice with force constant K is given by

$$(A) (\omega_f)_{\max} = \left[ 2K \left( \frac{1}{M} + \frac{1}{m} \right) \right]^{\frac{1}{2}}$$

$$(B) (\omega_f)_{\max} = \left[ K \left( \frac{1}{M} + \frac{1}{m} \right) \right]^{\frac{1}{2}}$$

$$(C) (\omega_f)_{\max} = \left[ \frac{2K}{M} \right]^{\frac{1}{2}}$$

$$(D) (\omega_f)_{\max} = \left[ \frac{2M}{K} \right]^{\frac{1}{2}}$$

98. Ionic crystals are excellent insulators at room temperature but become conductors at high temperatures because

- (A) The ions gain more electrons at higher temperatures
- (B) The crystal lattice breaks down, allowing ions to move freely
- (C) The covalent bonds between ions strengthen with heat
- (D) The electrons become more tightly bound to the nuclei at higher temperatures

99. For an electron moving in a one-dimensional periodic lattice of periodicity a, which of the following corresponds to an energy eigenstate consistent with Bloch's theorem ?

- (A)  $\psi(x) = A \exp(i\pi x/a) (\cos 2\pi x/a) + \cos(2\pi x/a)$
- (B)  $\psi(x) = A \exp(i\pi x/a)$
- (C)  $\psi(x) = A \exp(i2\pi x/a) + \cosh(2\pi x/a)$
- (D)  $\psi(x) = A \exp(i\pi x/2a) (\pi x/2a + i\pi/2a)$

100. The nature of the interaction that gives rise to the van der Waals force in a molecular crystal is

- (A) Dipolar
  - (B) Nuclear
  - (C) Magnetic
  - (D) Quadrupolar
-



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